

FINAL EXAM MATH 17B- No.1
Duration 75 minutes

Unauthorized materials

Exercise 1. Evaluate the following integrals.

- a) 2.0 pt (First make an appropriate substitution, and then use IBP) $\int_0^3 \sqrt{x+1} \ln \sqrt{x+1} dx$.
- b) 1.0 pt $\int_1^\infty \frac{1}{x^{\frac{3}{2}}} dx$.

Exercise 2. Denote by $L(t)$ the length of a fish at time t and assume that the fish grows according the von Bertalanffy equation

$$\frac{dL}{dt} = 2.2 (25 - L), \text{ with } L(0) = 5.$$

- a) 1.0 pt Solve the equation.
- b) 1.0 pt Find the length of the fish at time $t = 2$.
- c) 1.0 pt Find the asymptotic length of the fish, that is, find $\lim_{t \rightarrow \infty} L(t)$.

Exercise 3. Let $N(t)$ denote the size of a population at time t that satisfies the logistic equation

$$\frac{dN}{dt} = 4N\left(1 - \frac{N}{40}\right) - 2N := g(N), \text{ for } N \geq 0.$$

- a) 1.0 pt Graph $N(t)$.
- b) 3.0 pt Find all equilibria of the equation and determine their stability using both (i) the graphical approach, and (ii) the analytical approach.

FINAL EXAM MATH 17B- No.2
Duration 75 minutes

Unauthorized materials

Exercise 1. Evaluate the following integrals

- a) 2.0 pt (First make an appropriate substitution, and then use IBP) $\int_1^4 \sqrt{x} \ln \sqrt{x} dx$.
- b) 1.0 pt $\int_1^\infty \frac{1}{x^{\frac{4}{3}}} dx$.

Exercise 2. Denote by $L(t)$ the length of a fish at time t and assume that the fish grows according the von Bertalanffy equation

$$\frac{dL}{dt} = 1.8 (30 - L), \text{ with } L(0) = 8.$$

- a) 1.0 pt Solve the equation.
- b) 1.0 pt Find the length of the fish at time $t = 3$.
- c) 1.0 pt Find the asymptotic length of the fish, that is, find $\lim_{t \rightarrow \infty} L(t)$.

Exercise 3. Let $N(t)$ denote the size of a population at time t that satisfies the logistic equation

$$\frac{dN}{dt} = 3N\left(1 - \frac{N}{30}\right) - 2N := g(N), \text{ for } N \geq 0.$$

- a) 1.0 pt Graph $N(t)$.
- b) 3.0 pt Find all equilibria of the equation and determine their stability using both (i) the graphical approach, and (ii) the analytical approach.